

DEALING WITH MISSING OBSERVATIONS: MULTIPLE IMPUTATION

Missing observations or attrition are a common issue in empirical research. This post briefly discusses the method multiple imputation to deal with missing observations¹. Multiple imputation replaces every missing value of the variable with a list of simulated values. We can then run the required specification to estimate the parameter of interest using the imputed dataset.

To illustrate the method, I use data from a randomized controlled trial (RCT) conducted by Blattman et al. (2011, 2014). The data can be downloaded from Harvard Dataverse².

Step 1: Setting up the dataset

Suppose we are interested in investigating the impact of randomly assigned cash transfers (given at baseline) on migration (measured at endline). We can run a logistic regression since the outcome variable “migrate_e” is a binary variable that refers to whether the respondent has changed parish at endline, since baseline. However, after checking the data, we notice that the variable “migrate_e” has 161 missing observations.

Now, suppose we wish to impute those 161 observations for the “migrate_e” variable and then fit a logistic regression model with the complete dataset. To do so, we can use multiple imputation “mi” commands, which are readily available to use on Stata³. To use the commands, the dataset in memory should be set as an “mi” dataset, as shown in the second command below.

Variable	Obs	Mean	Std. dev.	Min	Max
treated	5,354	.4407919	.4965284	0	1
urban	5,354	.2099365	.4073011	0	1
age	5,354	24.95106	5.190868	14	59
age_2	5,354	649.4957	292.4608	196	3481
age_3	5,354	17697.34	13689.43	2744	205379
voc_training	5,354	.0765783	.2659459	0	1
migrate_e	5,193	.3672251	.482095	0	1
education	5,354	7.859171	2.938558	0	14
wealthindex	5,354	-.119519	.9905206	-2.322873	5.178377
risk_avers~n	5,354	-7.38e-09	1	-3.394701	1.391094

¹ Multiple imputation was first discussed in Rubin (1987).

² I am using the dataset “yop2_yop4_deid.dta”.

³ The Stata version used here is Stata 17.0.

```
. mi misstable summarize, all
```

Variable	Obs=.	Obs>.	Obs<.	Obs<.		
				Unique values	Min	Max
treated			5,354	2	0	1
urban			5,354	2	0	1
age			5,354	40	14	59
age_2			5,354	40	196	3481
age_3			5,354	40	2744	205379
voc_training			5,354	2	0	1
migrate_e	161		5,193	2	0	1
education			5,354	15	0	14
wealthindex			5,354	>500	-2.322873	5.178377
risk_avers~n			5,354	173	-3.394701	1.391094

The misstable summarize command is particularly useful when you have multiple variables with missing values.

Step 2: Imputing missing values

I impute the values for “migrate_e” using a logit regression since it is a binary variable. Refer to table 1 below for which commands to use after “mi impute” depending on the type of variable.

Table 1: Commands used for the different types of imputation variables.

Type of Variable	Commands for the relevant imputation method
Continuous	regress, pmm, truncreg, intreg
Binary	logit
Categorical	ologit, mlogit
Count	Poisson, nbreg

```
. mi impute regress migrate_e treated $controls, add(20) rseed(1234)
```

```
Univariate imputation          Imputations =      20
Linear regression              added =      20
Imputed: m=1 through m=20     updated =      0
```

Variable	Observations per m			Total
	Complete	Incomplete	Imputed	
migrate_e	5193	161	161	5354

(Complete + Incomplete = Total; Imputed is the minimum across m of the number of filled-in observations.)

I select the number of imputations to be equal to 20.⁴ For the results to be reproducible, select the random number seed. I selected 1234. Other control variables being used are “age age_2 age_3 urban risk_aversion education wealthindex voc_training.”⁵

Now, we are ready to estimate our logistic regression as shown below. Remember to look at the imputed values of the “migrate_e” and make sure they make sense. Notice that the number of observations is now 5,354.

Step 3: Estimating the model using imputed datasets

The mi estimate command estimates the desired model with each of the 20 imputed datasets (where 20 is the number of imputations decided by the researcher) and attains 20 respective coefficients with their corresponding standard errors. Stata combines these 20 estimates to attain one coefficient, standard error, and set of inferential statistics.

```
. mi estimate : logistic migrate_e treated $controls
```

Multiple-imputation estimates		Imputations		=		20	
Logistic regression		Number of obs		=		5,354	
		Average RVI		=		0.0000	
		Largest FMI		=		0.0000	
DF adjustment: Large sample		DF: min		=		.	
		avg		=		.	
		max		=		.	
Model F test: Equal FMI		F(9, .)		=		16.19	
Within VCE type: OIM		Prob > F		=		0.0000	

migrate_e	Coefficient	Std. err.	t	P> t	[95% conf. interval]	
treated	.0662572	.0575711	1.15	0.250	-.04658	.1790944
age	.3068913	.1318661	2.33	0.020	.0484385	.5653441
age_2	-.0112538	.0043636	-2.58	0.010	-.0198063	-.0027013
age_3	.0001161	.0000455	2.55	0.011	.0000268	.0002053
urban	.6880293	.0696607	9.88	0.000	.5514967	.8245619
risk_aversion	.0352542	.0289156	1.22	0.223	-.0214194	.0919277
education	-.0084242	.0101639	-0.83	0.407	-.0283451	.0114966
wealthindex	.0625688	.0297909	2.10	0.036	.0041797	.1209579
voc_training	-.1548266	.1099523	-1.41	0.159	-.3703291	.0606758
_cons	-2.96503	1.261716	-2.35	0.019	-5.437948	-.4921122

To sum up the steps that were implemented above:

- 1) Select the data you want to use, load it, and set it for use with “mi”.
- 2) Check which variables contain missing observations and thus those that need to be imputed.
- 3) Select the imputation method depending on the type of the variable to be imputed. For example, use standard OLS for a continuous variable.
- 4) Select the number of imputations. T. Von Hippel (2020) provide details on how many imputations should be chosen.
- 5) Select the random number seed for the results to be reproducible.
- 6) Impute the missing values of the variable(s) using mi impute.
- 7) Estimate the desired model using mi estimate.

⁴ This is selected arbitrarily here, but this number could be given more thought. Check, for example, T. Von Hippel (2020) for more details on how many imputations you need.

⁵ All control variables are baseline variables. “age” is the age of the respondent, “age_2” is is age to the power 2, “age_3” is age to the power 3, “urban” is a binary variable for whether one lives in an urban or rural area, “risk_aversion” is an index that indicated the risk aversion of an individual (all indices are calculated based on a set of survey questions), “education” demonstrated the highest level of education reached at school, “wealthindex” is an index that indicated the respondent’s wealth, “voc_training” is a binary variable indicating whether the respondent has had any vocational training.

References:

Blattman, Christopher; Fiala, Nathan; Martinez, Sebastian, 2014, "Northern Uganda Social Action Fund - Youth Opportunities Program", <https://doi.org/10.7910/DVN/27898>, Harvard Dataverse, V1.

Blattman, Christopher; Fiala, Nathan; Martinez, Sebastian, 2019, "The long term impacts of grants on poverty: 9-year evidence from Uganda's Youth Opportunities Program", <https://doi.org/10.7910/DVN/V0N0HA>, Harvard Dataverse, V1.

Stata. 2021. "Multiple-Imputation Reference Manual," 388.